## ACO Algorithm with Additional Reinforcement

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The aim of the paper is to develop the functionality of the ant colony optimization (ACO) algorithms by adding some diversification such as additional reinforcement of the pheromone. This diversification guides the search to areas in the search space which have not been yet explored and forces the ants to search for better solutions. In the ACO algorithms [1, 2] after the initialization, a main loop is repeated until a termination condition is met. In the beginning ants construct feasible solutions, then the pheromone trails are updated. Partial solutions are seen as states: each ant moves from a state i to another state j corresponding to a more complete partial solution. For ant k, the probability  $p_{ij}^k$  of movement from state i to a state j as a next state is given as:

$$p_{ij}^{k} = \begin{cases} \frac{\tau_{ij}\eta_{ij}^{\beta}}{\sum_{l \in allowed_{k}} \tau_{il}\eta_{il}^{\beta}} & \text{if } j \in allowed_{k} \\ 0 & \text{otherwise} \end{cases} , \tag{1}$$

where  $\tau_{ij}$  is a pheromone level corresponding to this movement,  $\eta_{ij}$  is the heuristic information and  $allowed_k$  is the set of remaining feasible states.

In the beginning initial pheromone level is set to be  $\tau_0$ . After all ants have completed their tours, the pheromone level is updated as follows:

$$\tau_{ij} \leftarrow \rho \tau_{ij} + \Delta \tau_{ij} \tag{2}$$

where  $0 < \rho < 1$  is a pheromone decay parameter and  $\Delta \tau_{ij}$  is different for different ACO algorithms.

When we perform the ACO algorithm search stagnation may occur. This can be happen, if the pheromone trail is significantly higher for one choice than for all others. The main purpose of this research is to avoid the stagnation situations by using additional reinforcement for unused movements and to search for better solutions. If some movement is not used in current tour we use additional pheromone reinforcement as follows:

$$\tau_{ij} \leftarrow \tau_{ij} + q\tau_{max},\tag{3}$$

where  $q \geq 0$  is a parameter and  $\tau_{max}$  is a maximal amount of the pheromone. After additional reinforcement unused movements have great amount of pheromone than used one which, belong to the poor solutions and less to used movements that belong to best solution. Thus, we force ants to choose new direction of search space without repeating the bad experience. Preliminary results for the traveling salesman problem (TSP) suggest the usefulness of above diversification. Table 1 shows a comparison between our ACO algorithm with additional reinforcement and MMAS. We use a particular implementation of ACO algorithm,

known as ant system with an elitist ant. Set of TSP from TSPLIB benchmark library (http://www.iwr.uniheidelberg.de/iw/compt/software/TSLIB95) is used as a test problems. The selected parameters for the test are , m=25 ants,  $\rho=0.8,$   $\beta=2$  and q=0.2. The maximum number of cycles was set to 20000 for all experiments and the average are taken over 25 trials. For comparison, the same program is used for both algorithms, with same parameters and same number of iterations and the difference is only in the pheromone updating. Bold numbers indicate the better results. From the achieved result of table 1, it is clear that our ACO algorithm with additional reinforcement performs better than MMAS. For future research is to develop this new ACO algorithm and test on different optimization problems.

Table 1. The results of ACO algorithm with additional reinforcement and MMAS algorithm

	Add. Reinforcement		MMAS	
Instance	Best	Average	Best	Average
d198	15780	15780.3	15780	15780.9
lin318	42029	42051.8	42029	42051.8
pcb442	50785	507891	50795	509421
att532	27686	27706.8	27693	27707.4
rat783	8808	8820	8808	8841
dsj1000	18688548	18704977.1	18708266	18736562.2
pr1002	259167	259692.5	259290	260025
${ m vm}1084$	239321	239434	239321	239490.17
pcb1173	56897	56970.5	56909	56969.4
d1291	50801	50820	50801	50847.7
rl1304	252948	253159	252948	253528.17
rl1323	270226	270580.17	270281	270725.5
fl1400	20161	20229.67	20254	20299.17
fl1577	22337	22412.83	22349	22423.67
vm1748	336873	337107.17	337506	337772.83
u1817	57294	57346.5	57314	57458.67
rl1889	317430	317743.33	318284	319295

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